

NOTES 2.7

TRANSITIVE & SUBSTITUTION
PROPERTIES

Transitive Property

- If **two** quantities are equal (or congruent) to the **same quantity**, then they are equal (or congruent) to each other.

Transitive Property

- Notice: Transitive is much like the Chain Reasoning....
- John is taller than Kevin and Kevin is taller than Louis.
- How do the heights of John and Louis compare?

Transitive Property

- EQUALITY EXAMPLE: If $AB = CD$ and $CD = EF$, then $AB = EF$
- CONGRUENCE EXAMPLE: If $\angle X \cong \angle Y$ and $\angle Y \cong \angle Z$,
then $\angle X \cong \angle Z$

Substitution Property

- This is when an equivalent amount (or measure) may **replace** another expression in an equation (or congruence situation).
 - we may only substitute equals in equations,
 - we do NOT have a substitution property of congruence.
- EQUALITY EXAMPLE: If $a + 4 = b$ and $a = 5$, then $5 + 4 = b$
- CONGRUENCE EXAMPLE: $m \angle X + m \angle Y = 90^\circ$ and $m \angle X = 30^\circ$,
then $30^\circ + m \angle Y = 90^\circ$.

Example # 1

Transitive or Substitution?

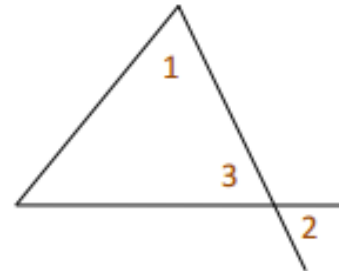
Example #1

Given: $\angle 1 \cong \angle 2$

$\angle 2 \cong \angle 3$

Concl: $\angle 1 \cong \angle 3$

Reason: ?



Solution: **Transitive Property**. Since both angles 1 and 2 are congruent to the same angle (angle 2), they must be congruent to each other.

Example # 2

Transitive or Substitution?

Example #2

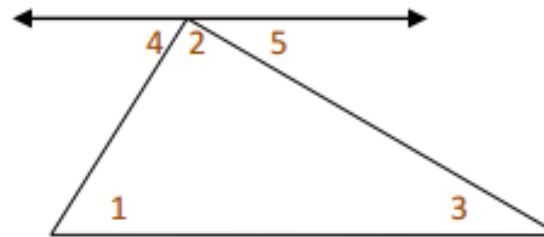
Given: $m\angle 1 \cong m\angle 4$,

$m\angle 3 \cong m\angle 5$,

$m\angle 4 + m\angle 2 + m\angle 5 = 180$

Conclusion: $m\angle 1 + m\angle 2 + m\angle 3 = 180$

Reason: ?



Solution: **Substitution Property.** In the equation stated lastly in the givens, the measures of angles 4 and 5 are replaced by their equals, the measures of angles 1 and 3, respectively.

Example # 3

Transitive or Substitution?

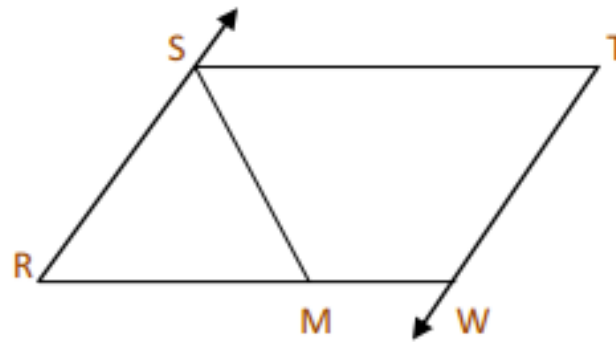
Example #3

Given: $RS = \underline{SM}$ (equation 1)

$TW = \underline{SM}$ (equation 2)

Conclusion: $RS = TW$

Reason: ?



Solution: Transitive or Substitution. Could be either one due to $=$.

Example # 4

Transitive or Substitution?

Example #4

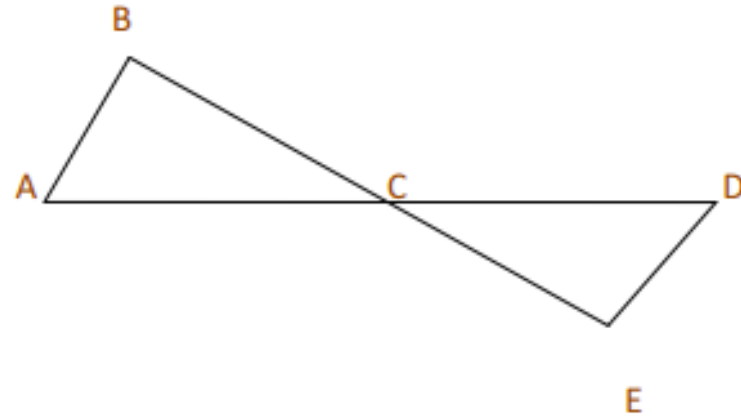
Given: C is the midpoint of \overline{AD}

$$AC = CE$$

Conclusion: $CD = CE$

Reason: ?

Solution: $AC = CD$, since point C is the midpoint of \overline{AD} .



We now have the set of relationships: $AC = CD$ (equation 1) $AC = CE$ (equation 2)

Since CD and CE are both equal to the same quantity (AC) they must be equal to each other. Therefore, $CD = CE$ by the transitive property of equality ~or~ We may replace AC by CE in Equation (1), also reaching the desired conclusion.